

# Measuring up the Competition: Neutron Scattering Studies of Antiferromagnetism in Cuprate Superconductors

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BCS@50  
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# Neutrons@75

*NATURE*

[FEBRUARY 27, 1932

## Possible Existence of a Neutron

IT has been shown by Bothe and others that beryllium when bombarded by  $\alpha$ -particles of polonium emits a radiation of great penetrating power, which has an absorption coefficient in lead of about  $0.3 \text{ (cm.)}^{-1}$ . Recently Mme. Curie-Joliot and M. Joliot found, when measuring the ionisation produced by this beryllium radiation in a vessel with a thin window, that the ionisation increased when matter containing hydrogen was placed in front of the window. The

It is to be expected that many of the effects of a neutron in passing through matter should resemble those of a quantum of high energy, and it is not easy to reach the final decision between the two hypotheses. Up to the present, all the evidence is in favour of the neutron, while the quantum hypothesis can only be upheld if the conservation of energy and momentum be relinquished at some point.

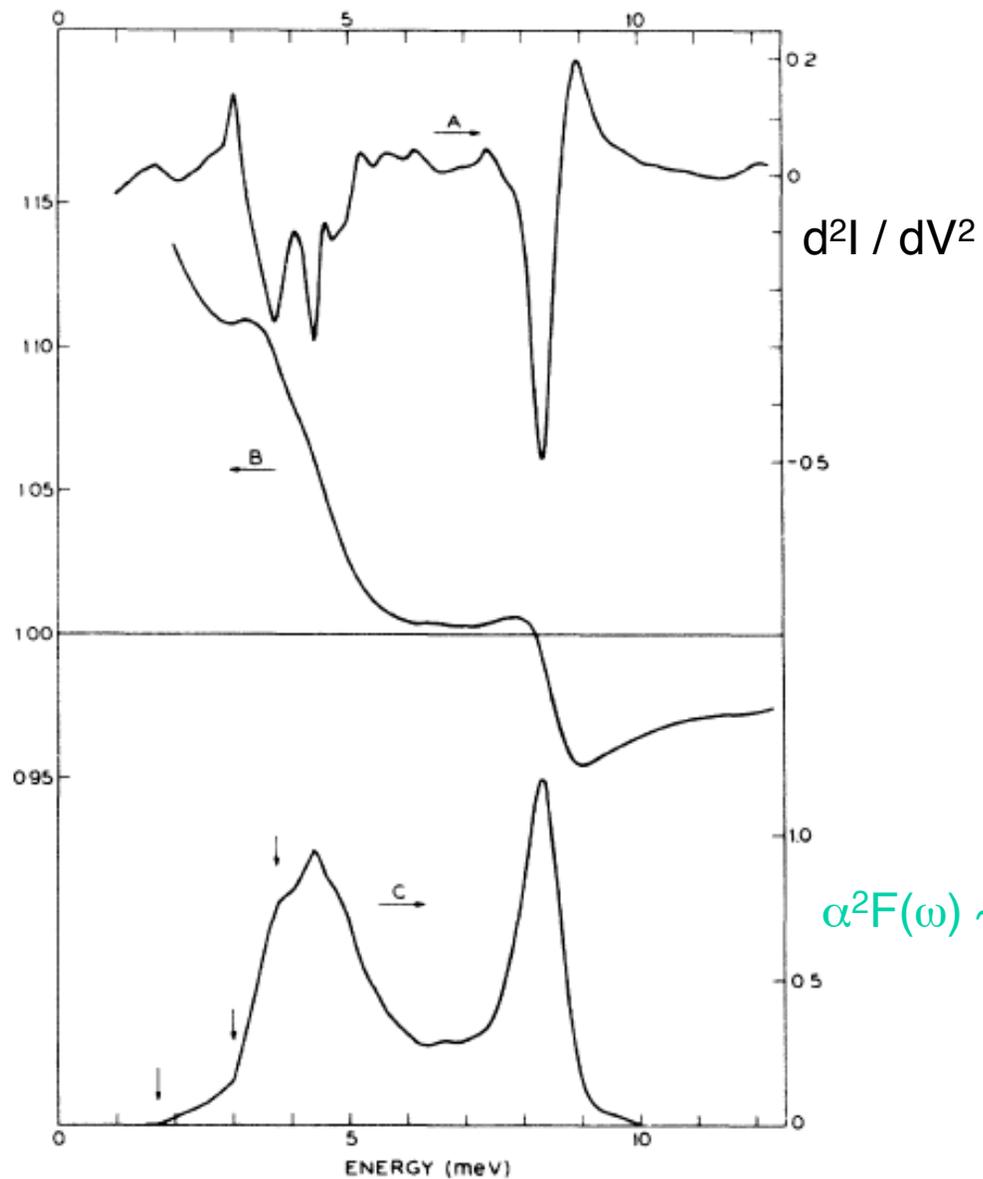
J. CHADWICK.

Cavendish Laboratory,  
Cambridge, Feb. 17.



James Chadwick

# McMillan-Rowell: $\alpha^2F(\omega)$ in Pb

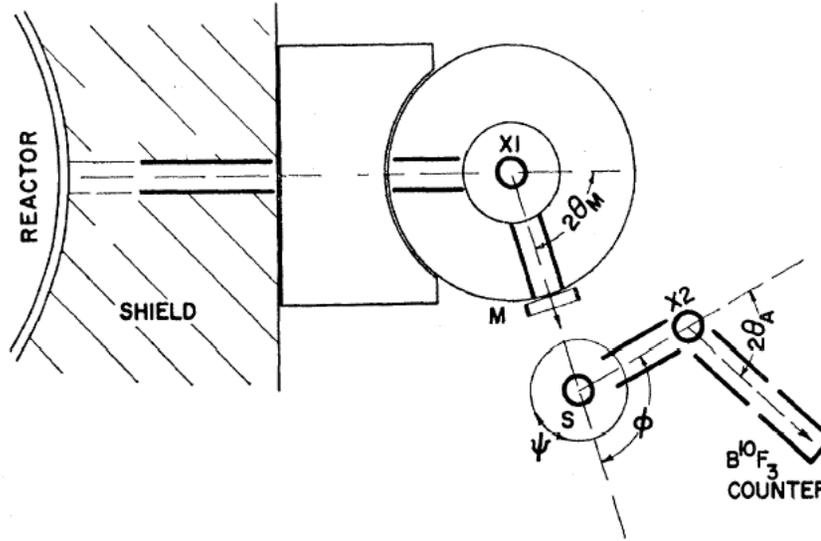
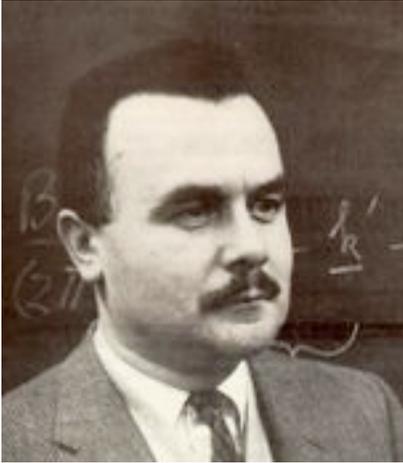


PRL 14, 108 (1965)

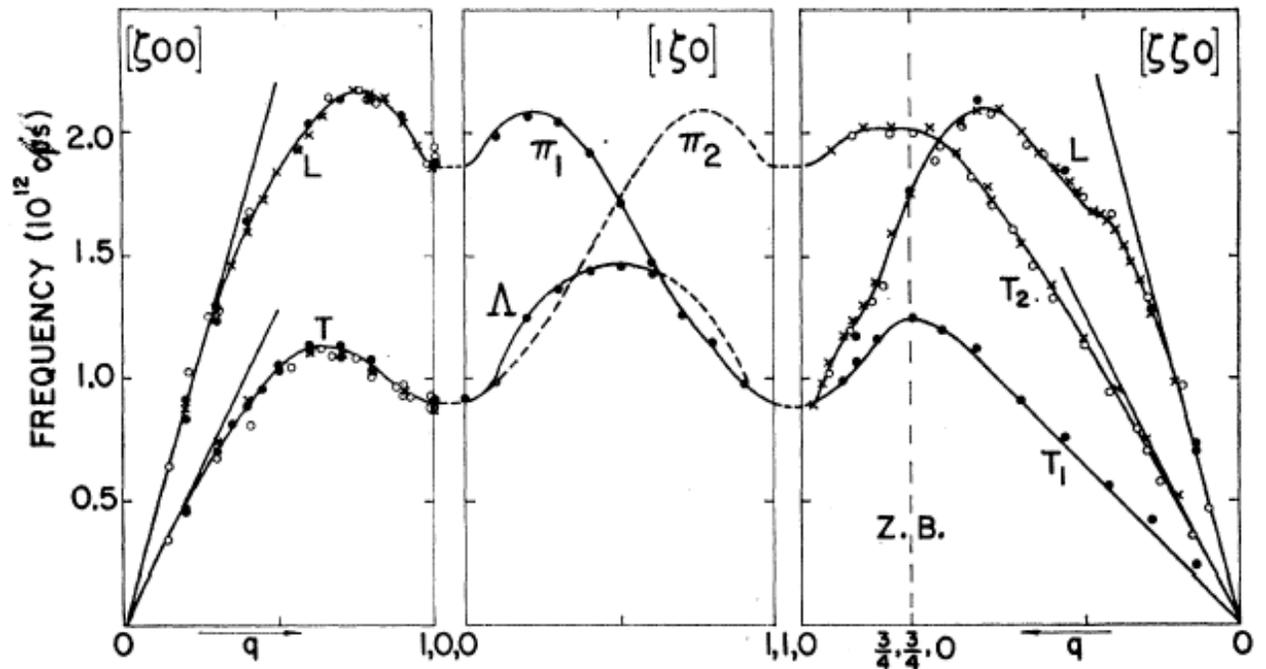
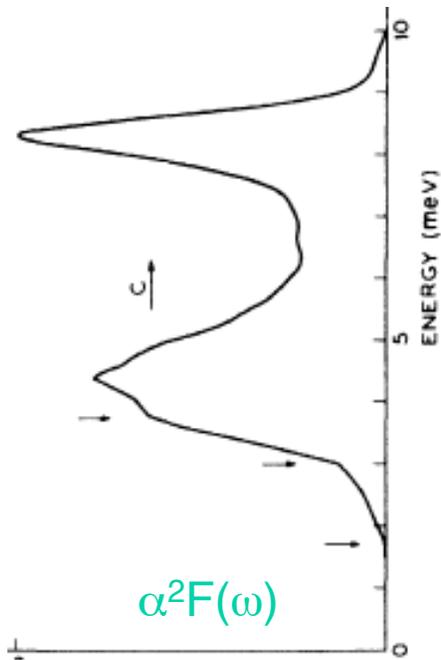
S-I-S tunnel junction

$\alpha^2F(\omega) \sim$  phonon density of states

# Brockhouse: Phonons in Pb

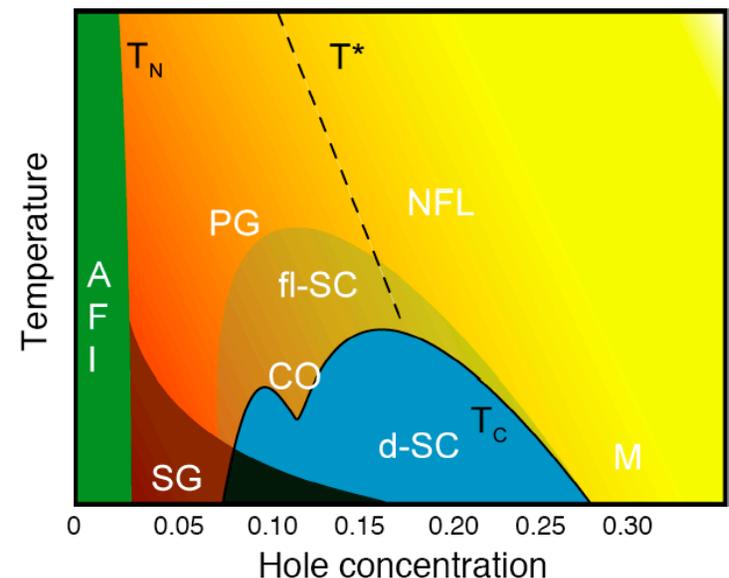


PR 128, 1099 (1962)



# Antiferromagnetism + Superconductivity in Cuprates

- Do spin waves replace phonons in pair formation?
  - Measure spectrum and compare with  $\alpha^2F(\omega)$ ?
- But what is the nature of the spin fluctuations?
- Does character of AF insulator survive into the SC regime?
  - If so, how do quasiparticles coexist?
- Does character change as soon as AF order is destroyed?
  - Is spin response due to quasiparticles?



# What Neutrons Tell Us

- Locally AF correlations survive through optimal doping
  - Effective superexchange energy softens with doping
- AF correlations disappear with overdoping
- SC can induce a gap in the spin fluctuation spectrum
  - But spin gap is not essential to SC
- Coexistence of local AF correlations and mobile holes
  - Stripes provide a proven motif for coexistence
  - Even ordered stripes are compatible with high-temperature SC

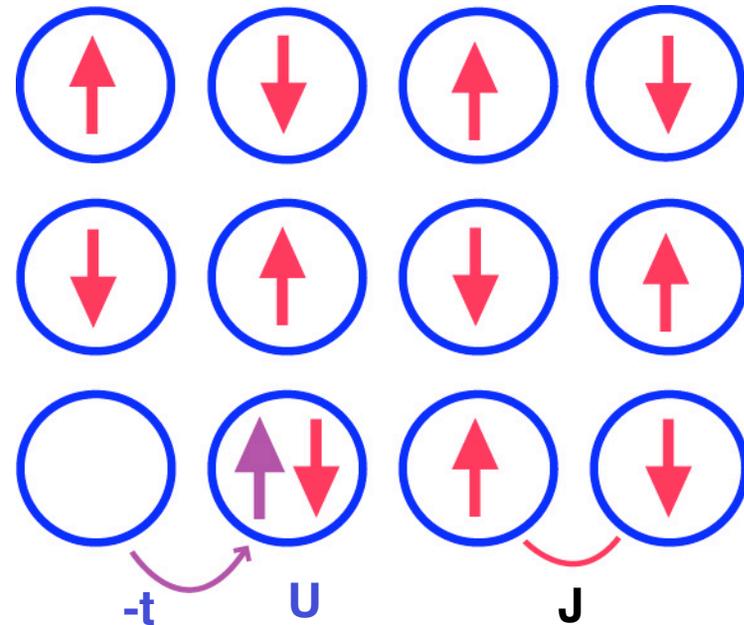
# 1/2-Filled Hubbard Model and Superexchange

1 orbital/site

1 electron/orbital

$t$  = kinetic energy

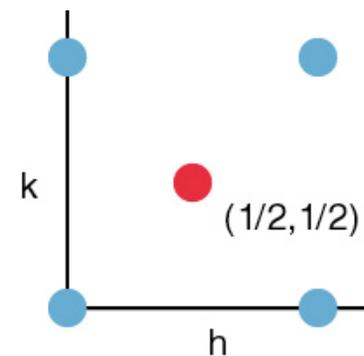
$U$  = onsite Coulomb repulsion



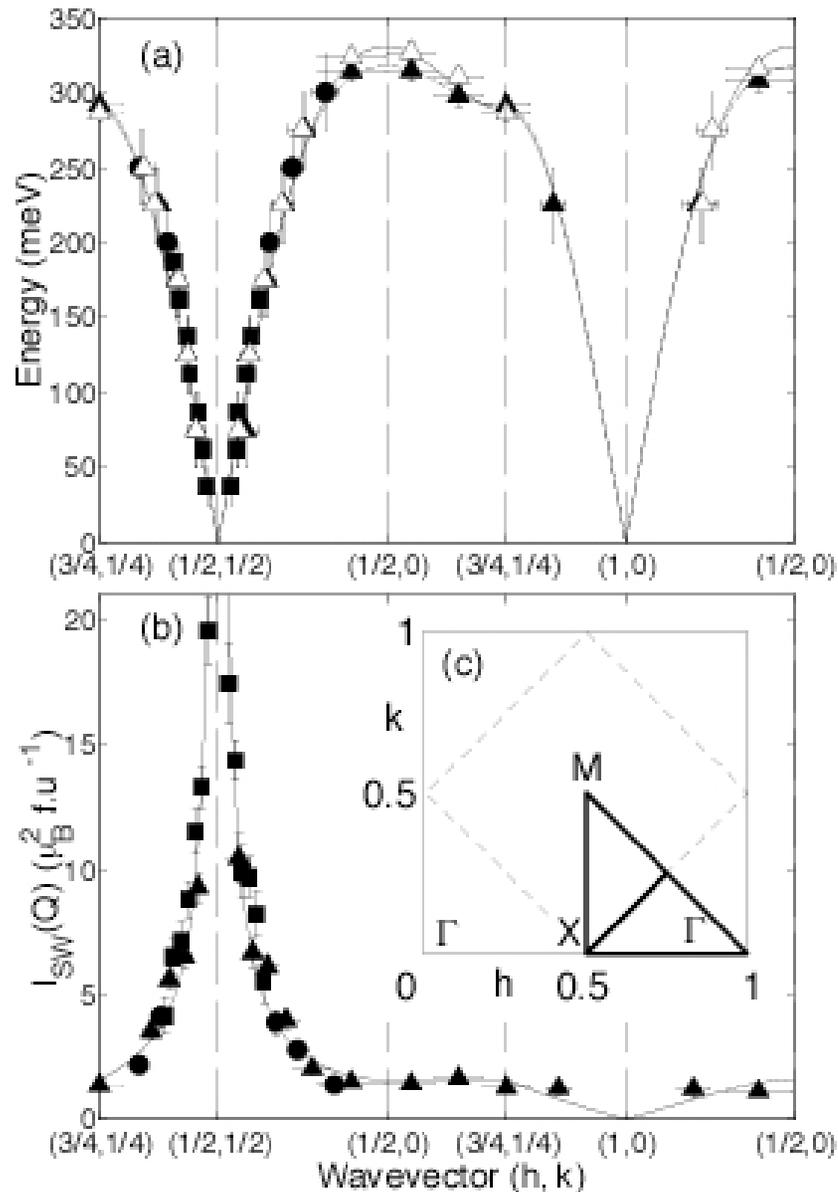
Coulomb repulsion  
+  
Pauli exclusion  
⇓  
Antiferromagnetic superexchange

$$J = 4t^2/U$$

P.W. Anderson (1959)



# Spin waves in antiferromagnetic $\text{La}_2\text{CuO}_4$



Coldea *et al.*  
PRL **86**, 5377 (2001)

Obtained by neutron  
scattering at ISIS

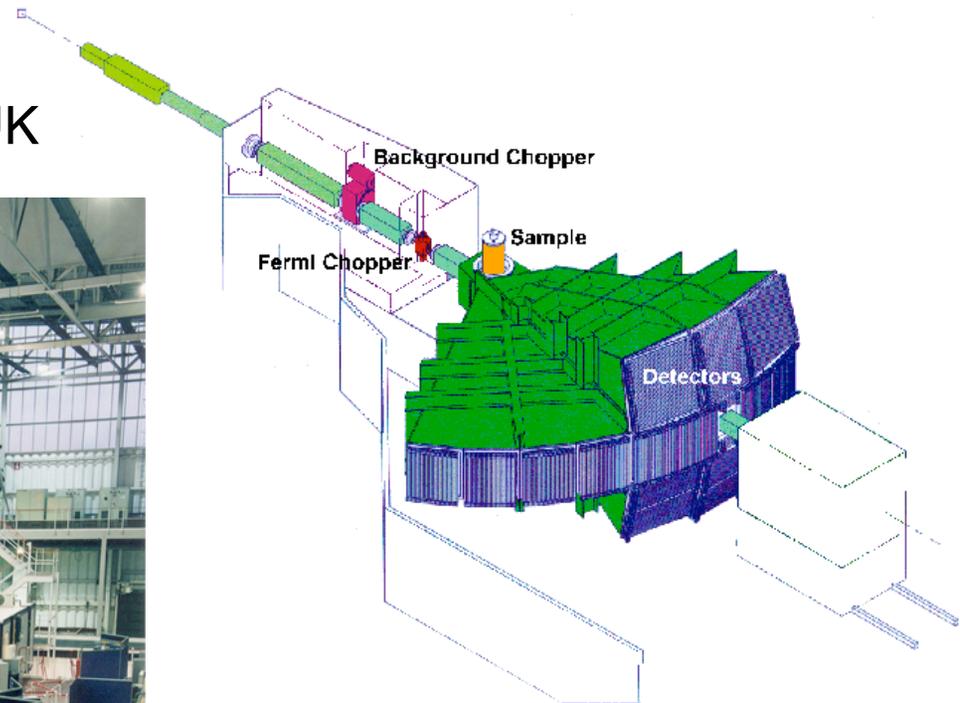
Well described by  
1/2-filled Hubbard model

Superexchange dominates

$J = 146 \text{ meV}$

# Neutron scattering studies using MAPS at ISIS

ISIS at Rutherford-Appleton Lab, UK



## MAPS

Time-of-flight spectrometer  
for study of inelastic scattering

Area detector: ~ 40,000 pixels  
2500 time channels

Toby Perring

# Constant-energy slices through magnetic scattering

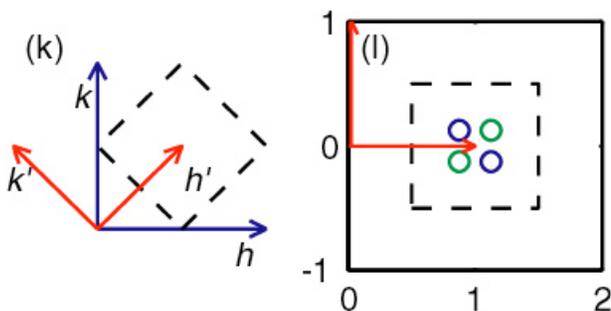
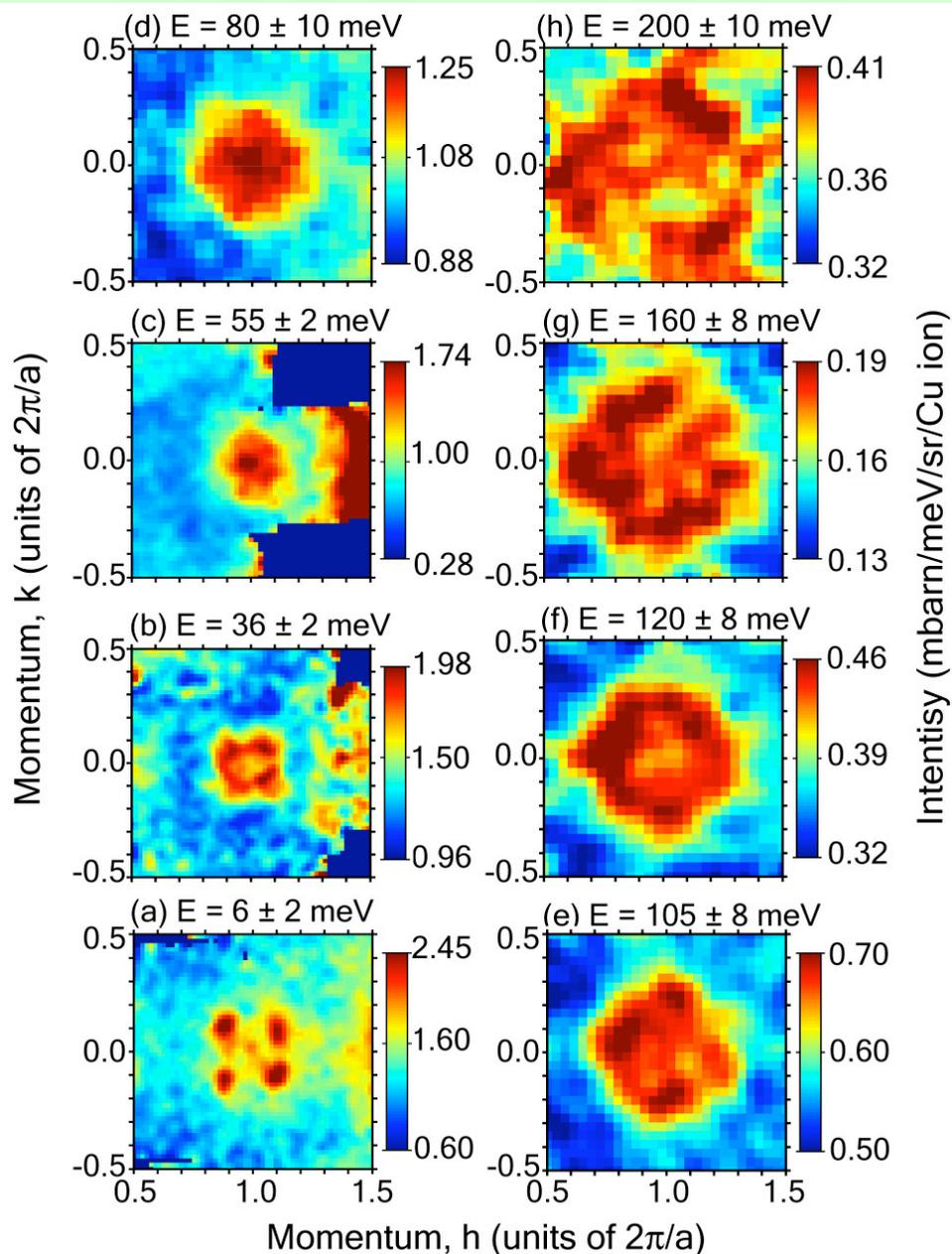
Stripe-ordered



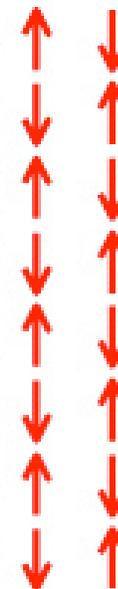
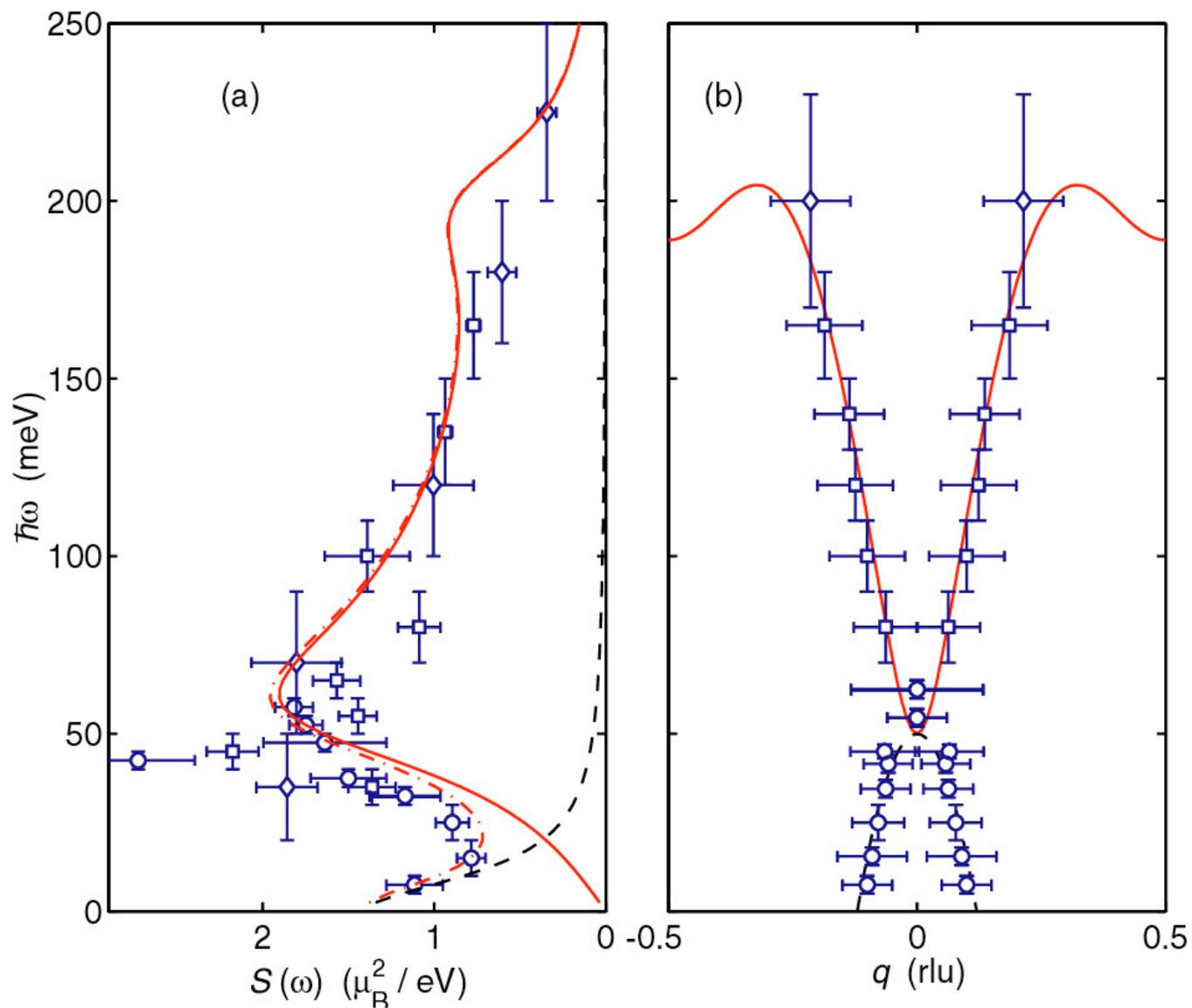
$T = 12 \text{ K}$

$T_c < 6 \text{ K}$

Nature **429**, 534 (2004)



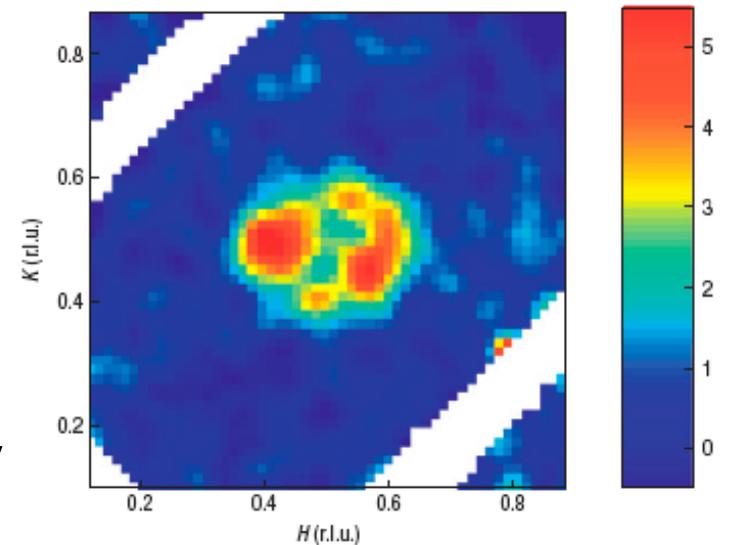
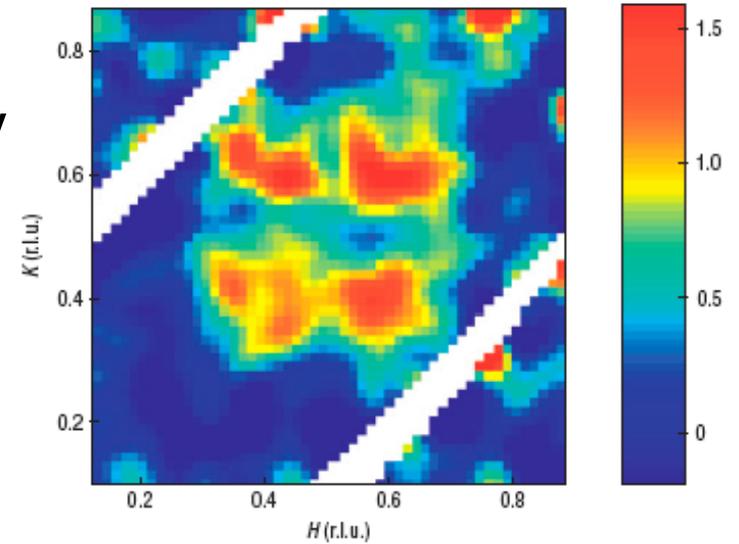
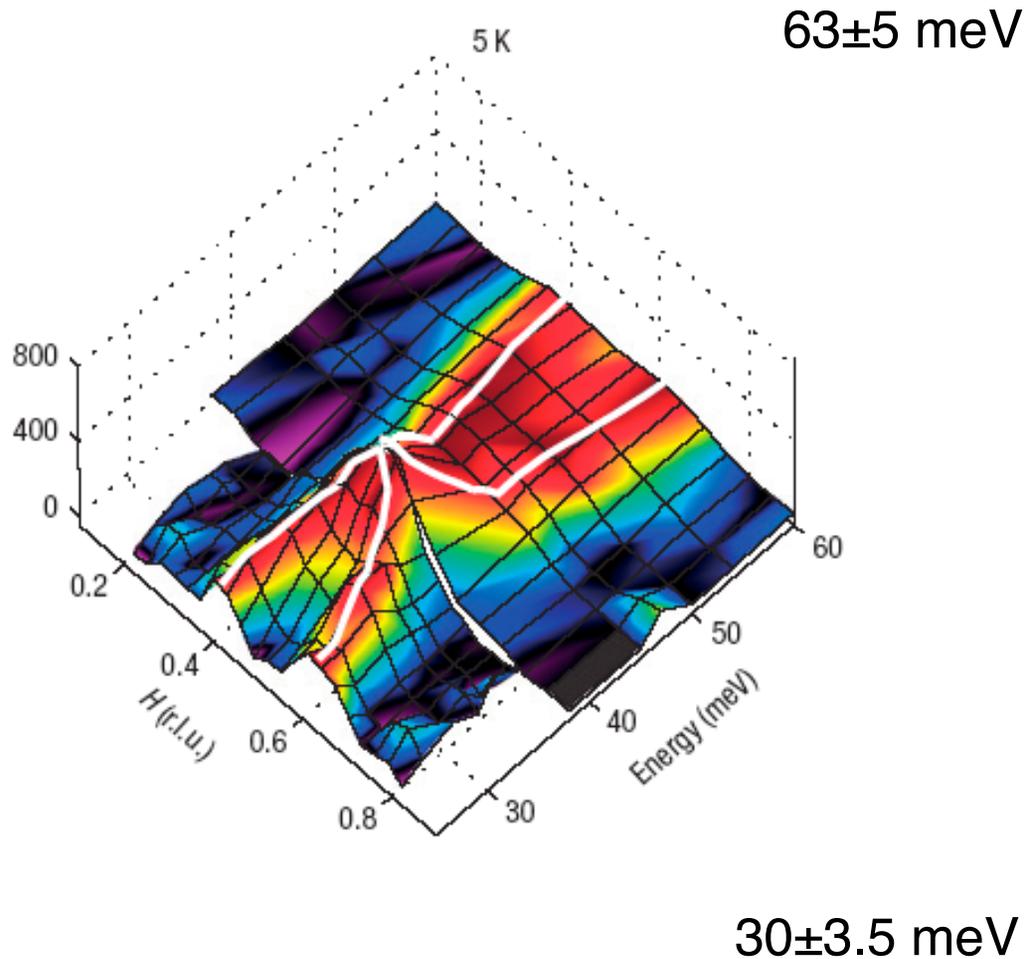
# $\text{La}_{1.875}\text{Ba}_{0.125}\text{CuO}_4$ spectrum



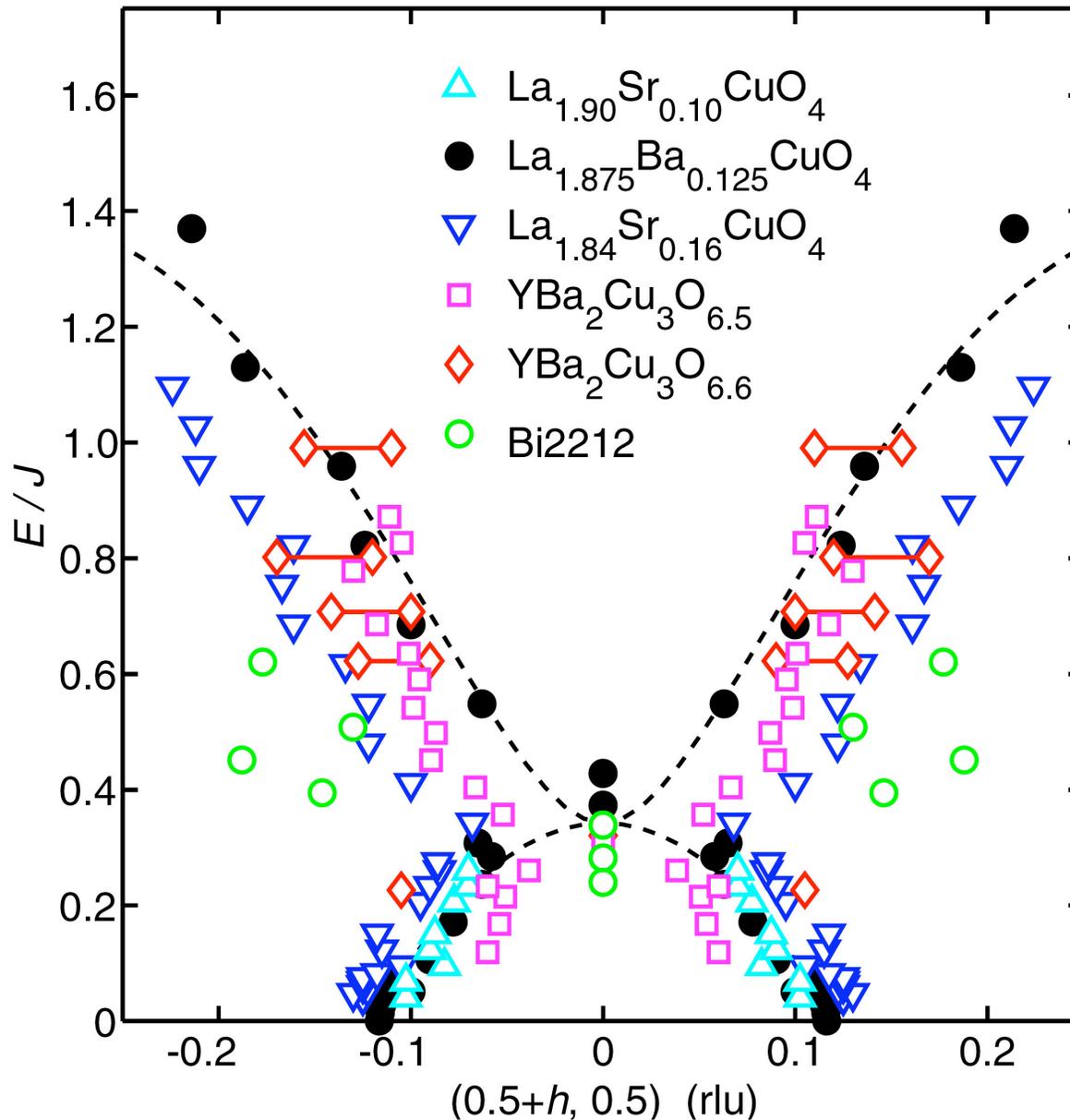
$J = 100 \text{ meV}$

# De-twinned $\text{YBa}_2\text{Cu}_3\text{O}_{6.6}$ $T_c = 61 \text{ K}$

Hinkov *et al.*, Nature Phys. (2007)



# Comparison of spin fluctuations in doped cuprates



LSCO	$J = 146$ meV
YBCO	$J = 106$ meV
Bi2212	$J \approx J_{\text{LSCO}}$

Christensen et al., PRL (2004)

Tranquada et al., Nature (2004)

Stock et al., PRB (2005)

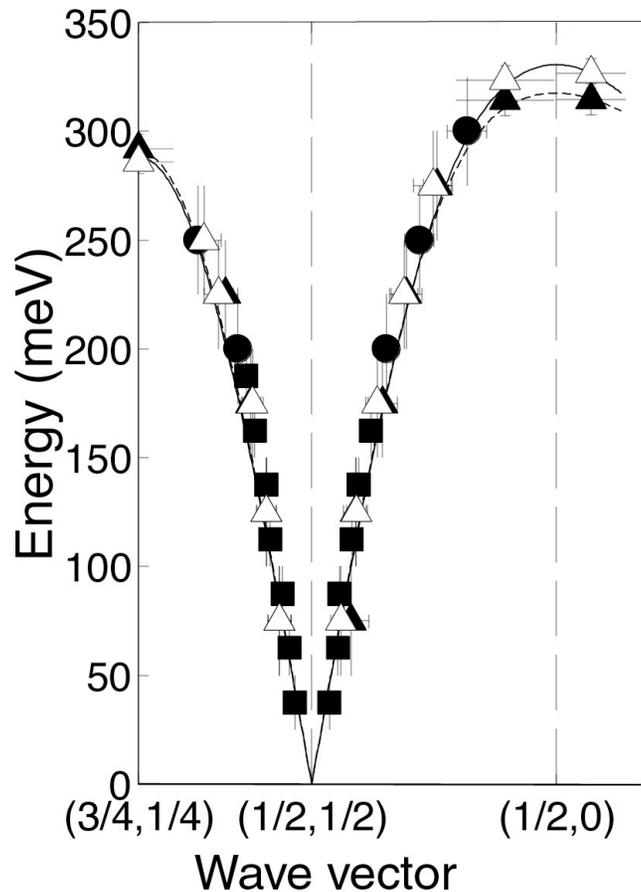
Hayden et al., Nature (2004)

Vignolle et al., Nature Phys. (2007)

G. Xu et al., (unpublished)

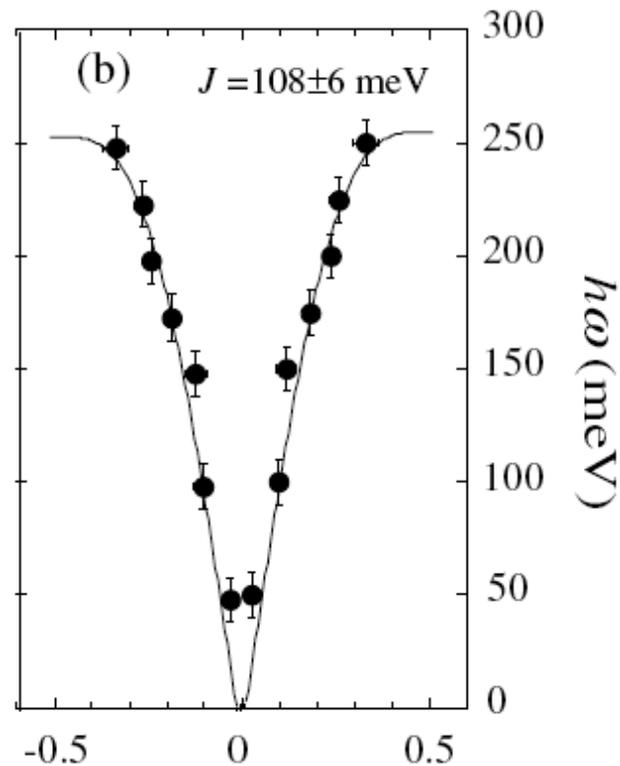
# Magnetic spectrum in $\text{La}_{2-x}(\text{Sr},\text{Ba})_x\text{CuO}_4$

$x = 0$



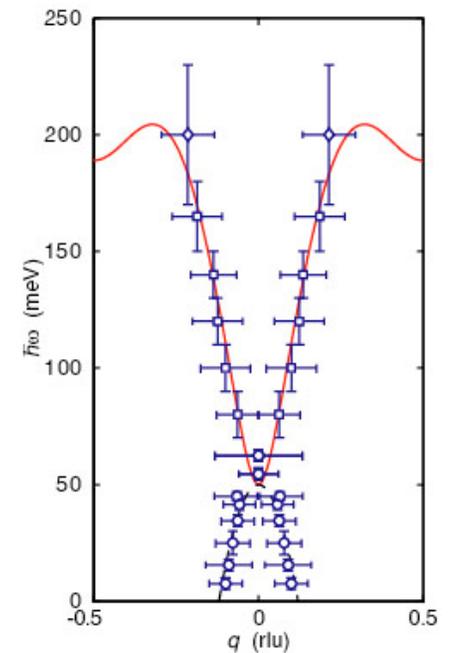
Coldea *et al.*, PRL (2001)

$x = 0.05$



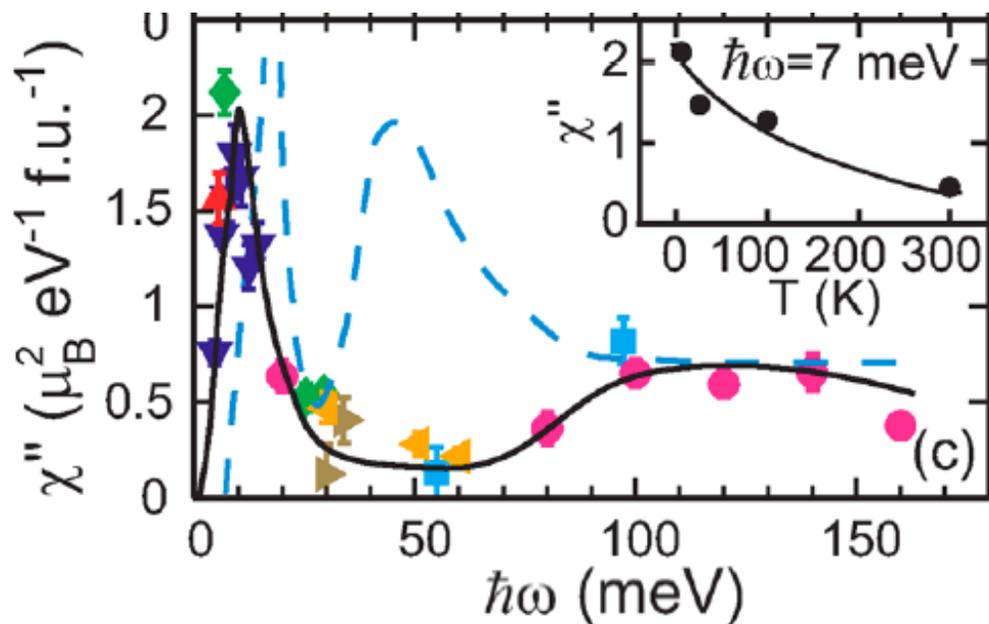
Goka *et al.*, Physica C (2003)

$x = 0.125$



Tranquada *et al.*, Nature (2004)

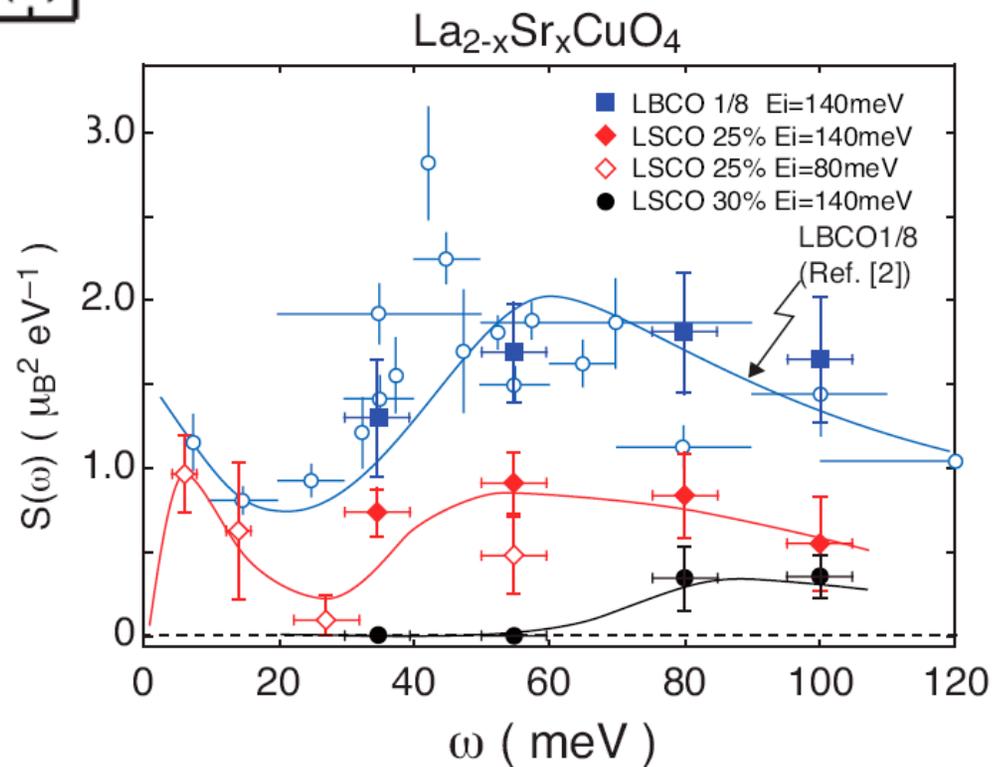
# Magnetic weight disappears with over-doping



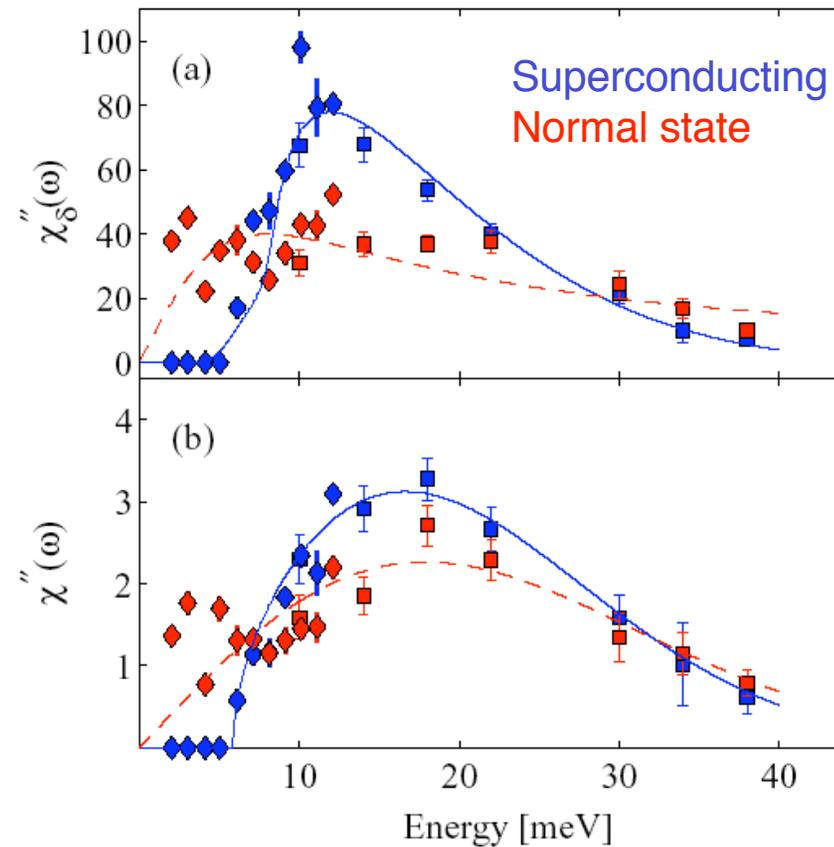
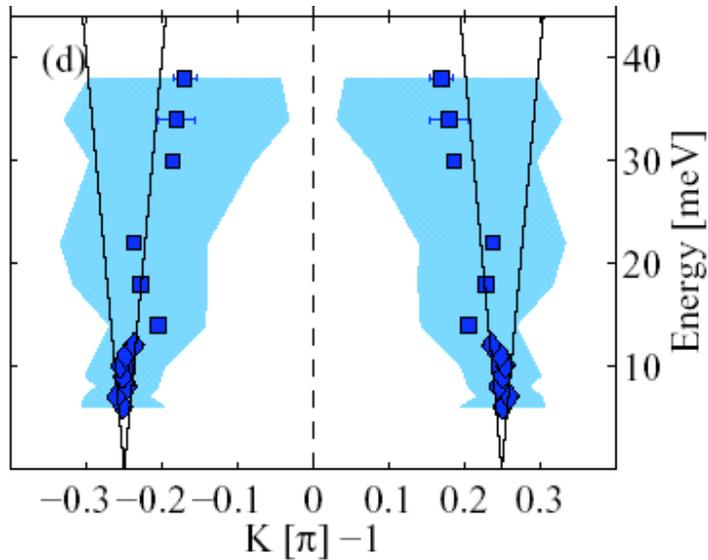
LSCO  $x = 0.22$

Lipscombe *et al.*, PRL (2007)

Wakimoto *et al.*, PRL (2007)

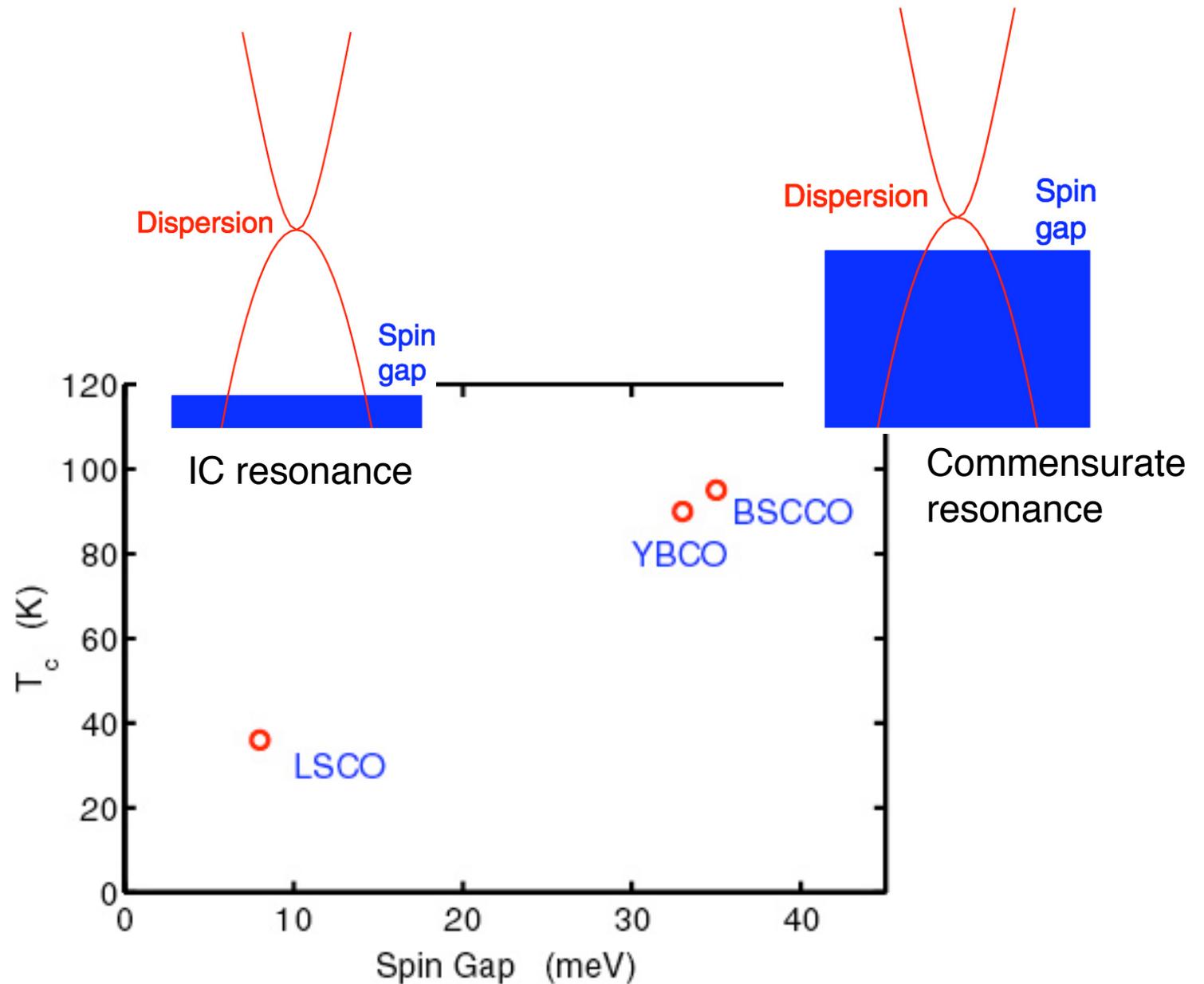


# Spin gap in $\text{La}_{2-x}\text{Sr}_x\text{CuO}_4$

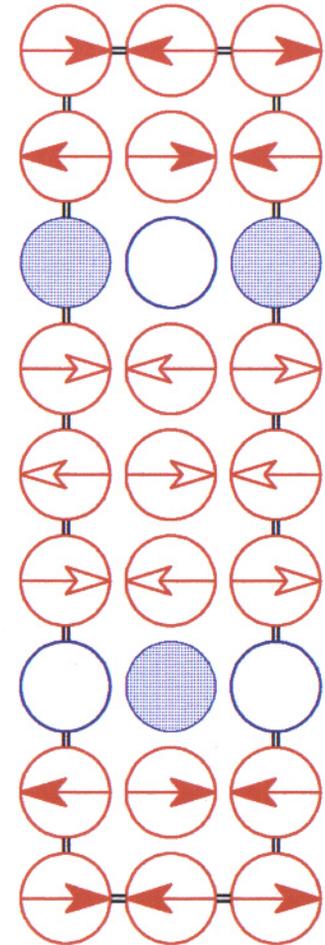
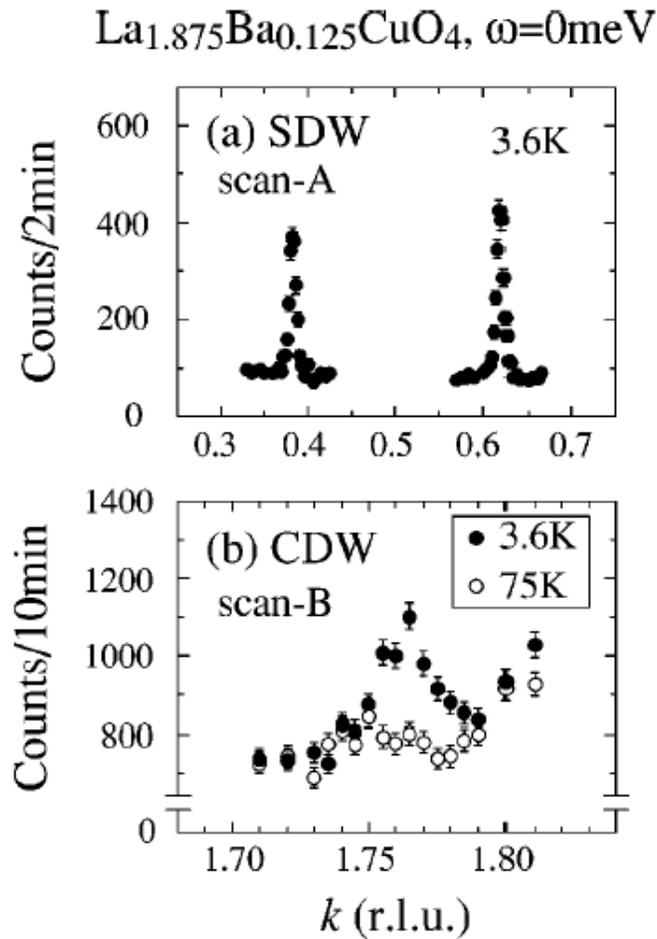
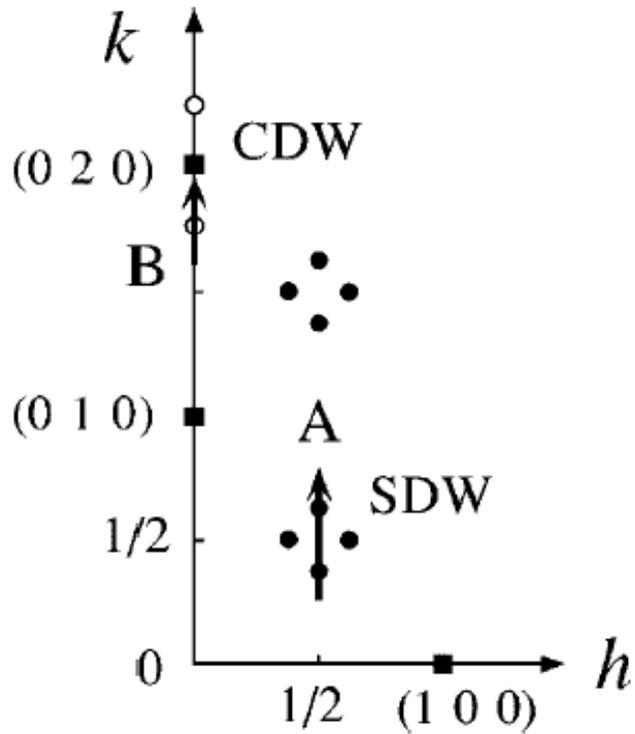


LSCO  $x = 0.16$   
Christensen *et al.*  
PRL **93**, 147002 (2004)

# Optimally-doped cuprates



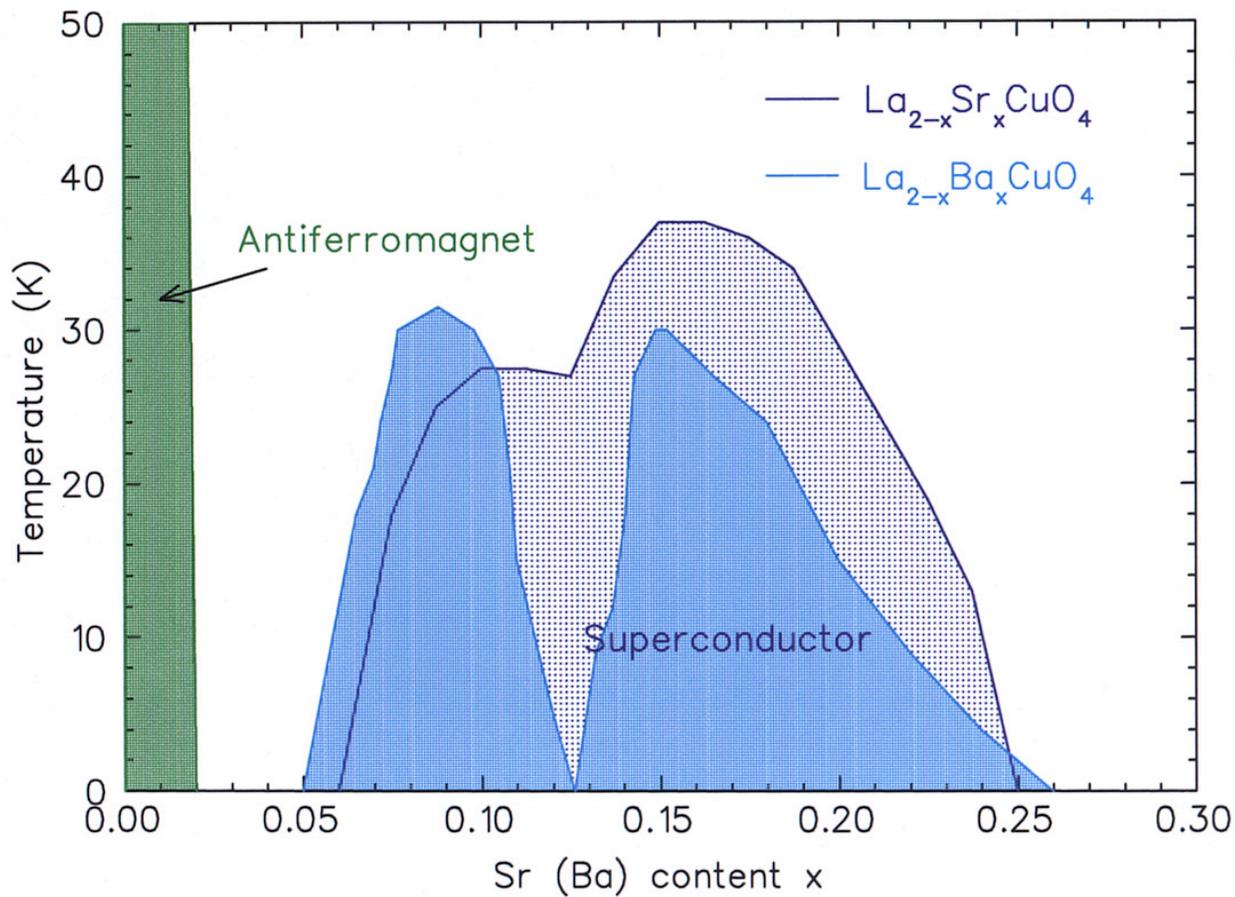
# Charge and spin stripe order in $\text{La}_{1.875}\text{Ba}_{0.125}\text{CuO}_4$



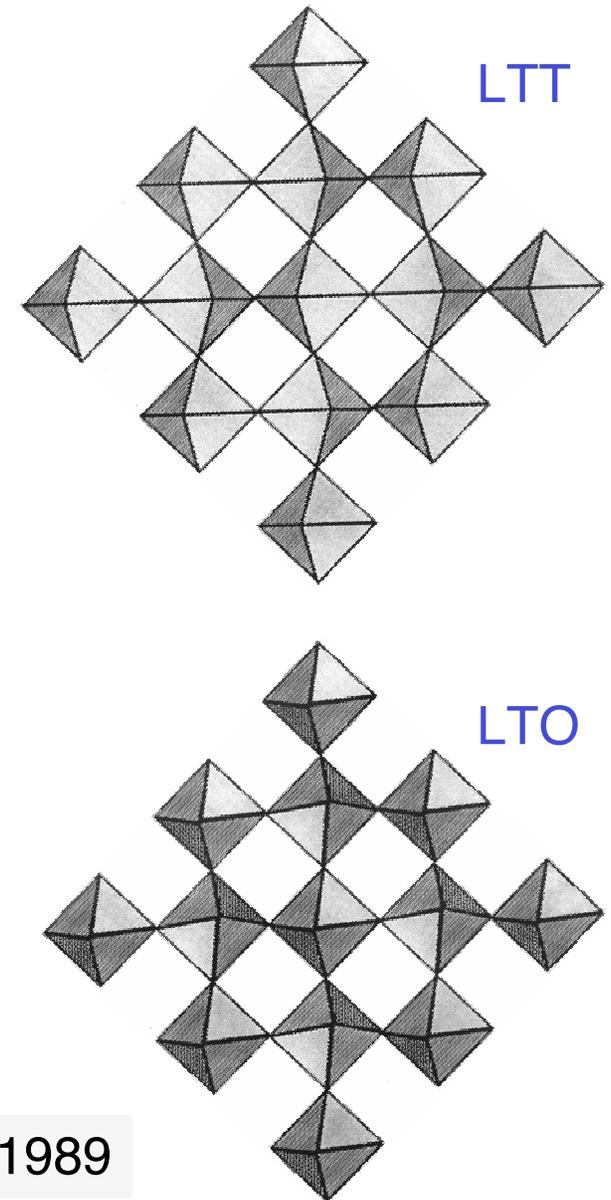
Fujita *et al.*, PRB (2004)

# $\text{La}_{2-x}\text{Ba}_x\text{CuO}_4$

1/8 problem



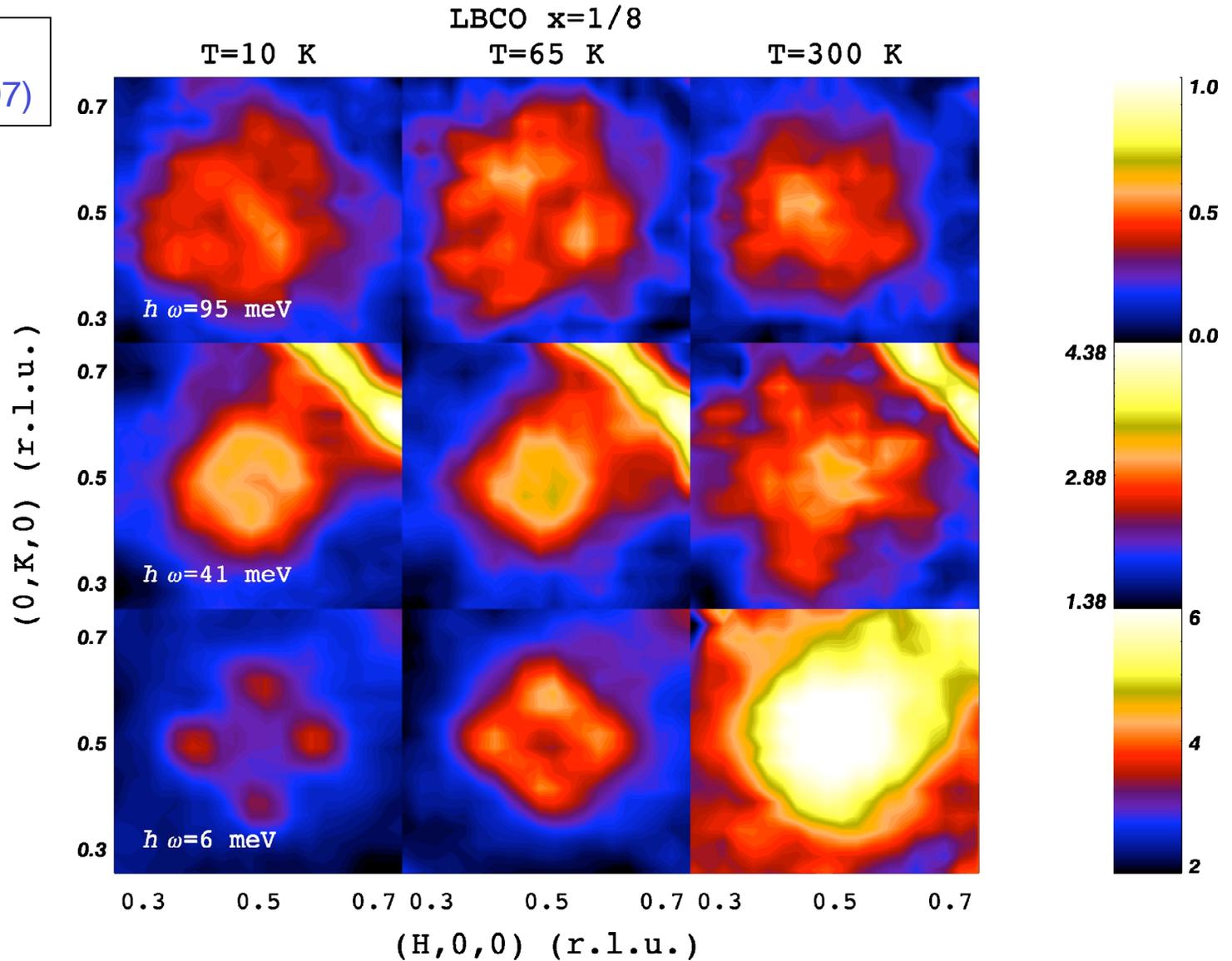
Moodenbaugh *et al.*, 1988



Axe *et al.*, 1989

# T-dependence of spin excitations in LBCO ( $x=1/8$ )

G. Xu *et al.*,  
Phys. Rev. B (2007)



Stripe order:	yes	no	no
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# Evidence for 2D superconducting fluctuations



$$\rho_c / \rho_{ab} > 10^4$$

for  $T < 40 \text{ K}$

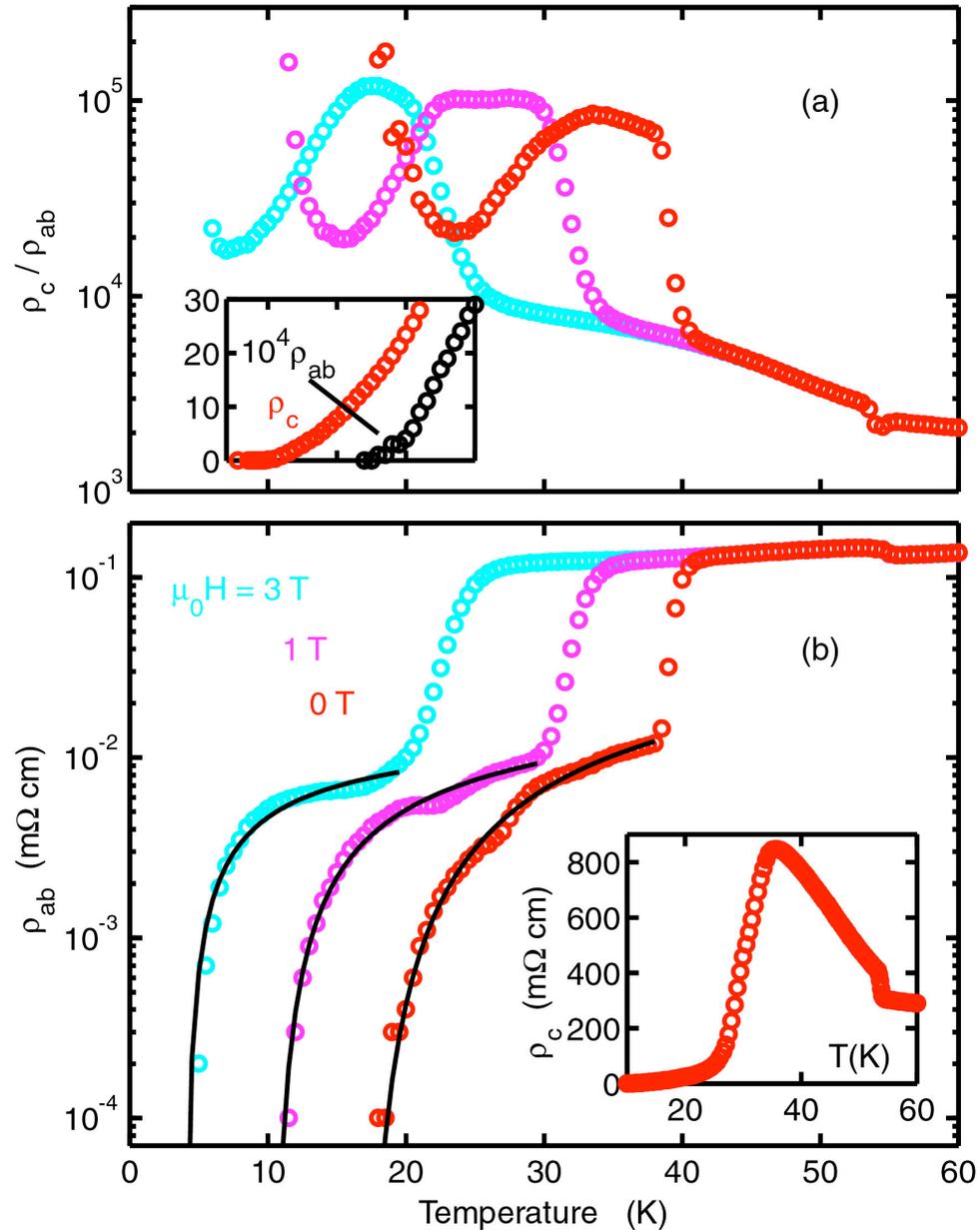
Q. Li *et al.*, PRL (2007)

Resistivity of a 2D superconductor  
for  $T > T_{KT}$ :

$$\rho = \rho_n \exp(a(T - T_{KT})^{-1/2})$$

Halperin + Nelson (1979)

$$T_{KT} = 16 \text{ K}$$



# Conclusions

- AF spin fluctuations in cuprate superconductors
  - Soften with doping
  - Disappear in the overdoped regime
- AF spin fluctuations are characteristic of the correlated insulator
- Stripes provide a way for AF character to survive in doped system
  - Stripe order is compatible with superconductivity